

Second Semester M.Sc. Degree Examination, July 2019

(CBCS Scheme)

Chemistry**Paper C 205 (Soft Core) – MATHEMATICS FOR CHEMISTS**

Time : 3 Hours

(Max. Marks : 70)

Instructions to Candidates : Answer Question No. 1 and any **FIVE** in the remaining.

1. Answer any **TEN** of the following. **(10 × 2 = 20)**
- Find a unit vector perpendicular to the vectors $\vec{m} = \hat{i} + 2\hat{k}$ and $\vec{n} = \hat{j} + 3\hat{k}$.
 - Find the angle between vectors $\vec{a} = (1, 2, 1)$ and $\vec{b} = (1, 3, 2)$.
 - If $A = \begin{bmatrix} 1 & -1 & 0 \\ 2 & 3 & 4 \\ 5 & 6 & 7 \end{bmatrix}$, find $A^T A$.
 - Find the eigen values of the matrix $A = \begin{bmatrix} 1 & 2 \\ 3 & 2 \end{bmatrix}$.
 - If $y = \sin^{-3}(x^2)$, find $\frac{dy}{dx}$.
 - If $x = a(t - \sin t)$, $y = a(1 - \cos t)$, find $\frac{dy}{dx}$ at $t = \pi/2$.
 - Find the critical points of the function $f(x) = x^4 - 4x^3 + 10$.
 - Find the integral $\int x^2 \sin(x) dx$.
 - If $Z = x^2 y^2 + 3xy$, find $\frac{\partial^2 z}{\partial x^2}$ and $\frac{\partial^2 z}{\partial y^2}$.
 - Solve the differential equation

$$x \frac{dy}{dx} + y = 0.$$
 - Solve the differential equation

$$y = e^{(A+B)x}$$
.
 - Three coins are tossed simultaneously, find the sample space.

2. (a) Prove that the triangle whose vertices are $3\hat{i} + 6\hat{j} - 3\hat{k}$, $2\hat{i} + 4\hat{j} - \hat{k}$ and $4(-\hat{i}) + \hat{k}$ is an isosceles right angled triangle.

- (b) Find the volume of the tetrahedron whose vertices are given by $(1, 1, 1)$, $(2, 1, 3)$, $(3, 2, 2)$ and $(3, 3, 4)$. (5 + 5)

3. (a) Find the values of x for which the matrix $\begin{bmatrix} 2 & 3 & 1 \\ x-1 & 2 & 3 \\ 1 & x & 5 \end{bmatrix}$ is singular.

- (b) Find the eigen values and eigen vectors of the matrix $\begin{bmatrix} 2 & -2 & 3 \\ 1 & 1 & 1 \\ 1 & 3 & -1 \end{bmatrix}$. (5 + 5)

4. (a) Solve by matrix method the system of equations

$$3x + y + 2z = 3$$

$$2x - 3y - z = -3$$

$$x + 2y + z = 4$$

- (b) Find the inverse of the matrix $\begin{bmatrix} -2 & 3 \\ 0 & 2 \\ -4 & 5 \end{bmatrix}$. (5 + 5)

5. (a) If $xy + 4y = 3x$: prove that $\frac{d^2y}{dx^2} = \frac{-24}{(x+4)^3}$.

- (b) If $x = at^2$, $y = 2at$, find $\frac{d^2y}{dx^2}$. (5 + 5)

6. (a) The volume of a sphere is increasing at the rate of 4π c.c per second. How fast the radius and surface area are increasing when the volume is 288π c.c?

- (b) Find the equation of tangent and normal to the curve $(1+x^2)y = 2-x$ where it crosses the x -axis. (5 + 5)

7. (a) Evaluate :

(i) $\int \frac{8 - 3t}{10t^2 + 13t - 3} dt$

(ii) $\int xe^x dx$

(b) Solve : $\frac{d^2y}{dx^2} - 18 \frac{dy}{dx} + 81y = 0$ (5 + 5)

8. (a) Find the Fourier series of the function $f(x) = x^2$ ($-\pi < x < \pi$)

(b) Fit a straight line for the following data

$x : 1 \ 2 \ 3 \ 4 \ 5$

$y : 8 \ 6 \ 5 \ 3 \ 1$